

# Numerical Modeling of an Automotive Derivative Polymer Electrolyte Membrane Fuel Cell Cogeneration System with Selective Membranes

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## Abstract

Cogeneration power plants based on fuel cells are a promising technology to produce electric and thermal energy with reduced costs and environmental impact. The most mature fuel cell technology for this kind of applications are polymer electrolyte membrane fuel cells, which require high-purity hydrogen.

The most common and least expensive way to produce hydrogen within today's energy infrastructure is through steam reforming of natural gas. Such a process produces a syngas rich in hydrogen that has to be purified to be properly used in low temperature fuel cells. However, the hydrogen production and purification processes strongly affect the performance, the cost, and the complexity of the whole energy system.

Purification is usually performed through pressure swing adsorption, which is a semi-batch process that increases the plant complexity and incorporates a substantial efficiency penalty. A promising alternative option for hydrogen purification is the use of selective metal membranes that can be integrated in the reactors of the fuel processing plant. Such a membrane separation may improve the thermo-chemical performance of the energy system, while reducing the power plant complexity, and potentially its cost. Herein, we perform a technical analysis, through thermo-chemical models, to evaluate the integration of Pd-based H<sub>2</sub>-selective membranes in different sections of the fuel processing plant: (i) steam reforming reactor, (ii) water gas shift reactor, (iii) at the outlet of the fuel processor as a separator device. The results show that a drastic fuel processing plant simplification is achievable by integrating the Pd-membranes in the water gas shift and reforming reactors. Moreover, the natural gas reforming membrane reactor yields significant efficiency improvements.

**Keywords:** CHP, Fuel Cell, Hydrogen, Membrane reactor

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## 1. Introduction

Residential and commercial buildings are responsible for 38.0% of the final energy consumed worldwide [1]. Moreover, about 30.0% of CO<sub>2</sub> emissions related to energy conversion [2] are caused by the building sector. The increase of households, the population rise, and the fragmentation of households will generate in the next years an increment in heating and cooling energy needs, and of electricity consumption, despite efficiency improvements in the final use [1–3]. In this scenario, Combined Heating and Power (CHP) could bring

relevant economical, environmental, and energetic advantages [4], such as: (i) higher total efficiency, thanks to thermal recovery [5, 6], (ii) less greenhouse gases and pollutants emissions [5, 7], (iii) deferring investment on large centralized power plants and distribution lines [5, 7], (iv) lower distribution losses [7], (v) ancillary service to the main electric energy distribution grid [7], (vi) optimal integration of new and alternative technologies, such as renewable energy sources [5, 8–11]. In particular [12]  $\mu$ -CHP ( $10^{-3}$  kW <  $P_{el}$  < 5 kW) and small-CHP ( $5$  kW <  $P_{el}$  <  $5 \times 10^3$  kW) systems are suitable for residential and commercial building applications and have a great innovation potential, given the large market size. In particular, only in the US, more than 1 Million new residential units are built every year [13] and the trend is positive again.

Fuel Cells (FCs) are an emerging technology in the stationary field, particularly for distributed CHP power

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## Nomenclature

$A$	Selective membranes surface	$\dot{m}_{H_2}$	Hydrogen mass flow rate
$A_{memb}^{SEP}$	Selective membranes surface for Plant B	$\dot{m}_{NG}$	Natural gas mass flow rate
$A_{memb}^{WGS}$	Selective membranes surface for Plant C	$\dot{m}_{NG}^{BURN}$	Natural gas mass flow rate to the burner
$A_{memb}^{REF}$	Selective membranes surface for Plant D	$\dot{m}_{NG}^{REF}$	Natural gas mass flow rate to the reformer
$dA$	Numerical-step for selective membranes surface	$\dot{m}$	Heat exchangers mass flow rate
CHP	Combined Heating and Power	$n$	Pressure exponent
$\Delta T_{ml}$	Logarithmic mean temperature difference	NG	Natural Gas
$\eta_{FC}$	Fuel Cell efficiency	$n_{H_2, syn}$	Initial number of $H_2$ moles in the syngas
$\eta_{fp}$	Fuel processor efficiency	$n_{tot}$	Total number of moles in the retentate
$\eta_{fp}^{tot}$	Fuel processor total efficiency	PEMFCs	Polymer Electrolyte Membrane Fuel Cells
$\eta_{glob}$	Global efficiency	$p^{REF}$	Reforming reactor pressure
$\eta^{is}$	Isoentropic efficiency of pumps or compressors	PSA	Pressure Swing Adsorption
$\eta^{SEP}$	Hydrogen separation efficiency	$P_{el}$	FC net electrical power
$\eta_{th}$	Thermal efficiency	$P_{el}^{nom}$	FC nominal net electrical power
FCH-JU	Fuel Cells and Hydrogen Joint Undertaking	$p_{H_2, perm}$	Hydrogen partial pressure on the permeate side
FCs	Fuel Cells	$p_{H_2, ret}$	Hydrogen partial pressure on the retentate side
$f^{syn}$	Initial syngas mole flow	$p_{perm}$	Total pressure on the permeate side
$f_{H_2}^{syn}$	Initial hydrogen mole flow	$p_{ret}$	Total pressure on the retentate side
$\Gamma$	Product of surface and thermal conductivity for heat exchangers	$\psi$	Ratio between the mass flow rates of the natural gas and of the steam entering the reformer
$h$	Fluids enthalpy	$Q$	Heat exchangers thermal power
HIWAR	Heat Integrated Wall Reactor	$Q_{cog}$	Cogeneration thermal power
$j_{H_2}$	Infinitesimal hydrogen permeation flux	$\Phi$	set-point
$J_{H_2}$	Hydrogen permeation flux	$T_{COG}$	Temperature of cogeneration water
$K_{H_2}$	Hydrogen permeance of the selective membrane	$T^{REF}$	Reforming reactor temperature
$K_{REF}$	Reforming chemical reaction equilibrium constant	WGS	Water Gas Shift
$K_{WGS}$	WGS chemical reaction equilibrium constant	$W_{aux}^{ref}$	Power required by the auxiliaries of the fuel processor
LHV <sub>H<sub>2</sub></sub>	Hydrogen lower heating value	$y_{H_2}$	Hydrogen concentration in the retentate
LHV <sub>NG</sub>	Natural gas lower heating value	$y_{H_2}^{min}$	Minimum hydrogen concentration in the retentate

plants in residential and commercial applications [14–19]. The most promising aspects of FCs for this application are: (i) the high efficiency [20], which is independent from the size and increases at part load [21–24], (ii) the low level of pollutant emission [25], (iii) the absence of moving parts that results in no noise and no vibrations [26]. It is not a case, in fact, that 64.0 % of the micro co-generation [12] units sold in 2012 are based on fuel cells [16, 27, 28].

Among the different kinds of fuel cells, Polymer Electrolyte Membrane Fuel Cells (PEMFCs) are technologically mature and provide several advantages [22–24]: (i) low operating temperature, (ii) fast start-up and regulation capability, (iii) high power density. Such characteristics make PEMFCs the most mature technology in the market. In fact, 75 % of new-installed FC units in 2017 were PEMFCs [29].

The high investment cost of FC-based CHP units is still the most relevant drawback with respect to conventional technologies. Commercial FC based small-CHP systems costs are far higher than the Fuel Cells and Hydrogen Joint Undertaking (FCH-JU) goals [30]. For energy systems with a nominal power in the range [5 kW<sub>el</sub> - 400 kW<sub>el</sub>] [31], the FCH-JU has set a cost target between 3500 €/kW<sub>el</sub> and 6500 €/kW<sub>el</sub>. For FCs the mobility market volume is much larger than the stationary sector. In fact, 68 % of the power of the FC energy systems developed in 2017 is attributable to transport applications [29]. As a consequence, the usage of automotive derivative PEMFCs for stationary systems can be an interesting option [32], being the cost of energy systems a decreasing function when the production volume increases [33–36]. The objective of the AutoRE project [32] is to build a constructive collaboration between the mobility and the stationary industrial sectors, in order to establish the basis for the commercialization of an automotive derivative PEMFC based CHP system with a capital cost of 2000 €/kW<sub>el</sub> and in the power range between 50 kW<sub>el</sub> and 100 kW<sub>el</sub> [32].

Nowadays, high-purity H<sub>2</sub> can be produced from hydrocarbons through the following steps [37]: (i) steam reforming, (ii) conversion of CO through the Water Gas Shift (WGS) reaction, (iii) final purification through Pressure Swing Adsorption (PSA). In such a fuel processing unit, the separation of H<sub>2</sub> can represent up to 50 % of the plant cost and significantly reduces the overall efficiency [38].

Dense metal membrane technology can be integrated into the H<sub>2</sub> production process in various ways, either with a WGS stage replacing the PSA process, or by direct integration in the reformer. The main benefit of the integration of a palladium membrane directly in a steam

reformer would be that the produced hydrogen is directly removed from the reaction zone at ultra-high purity, while additional purification steps are not required. Selective membranes can be made of several materials such as silica gel, zeolite, high temperature organic thermoplastic polymers and other metals such as aluminum [39–42], however here we focus on dense metal membranes made of Pd-Ag alloys, being the kind of technology most mature and the most suitable for our purposes.

Several studies have been performed in order to evaluate the integration of selective membranes in different parts of Natural Gas (NG) steam reforming based hydrogen production systems [43–47]. In this work we focus on the fuel processor of a 50 kW<sub>el</sub> CHP power plant based on low temperature automotive derivative PEMFCs. Such an application and such a power range are almost untapped. Moreover, we retrieve part load performance, in order to lay the foundation of a study considering the CHP system in a real energy management scenario.

Many studies focus on the single component development for membrane reactors using several experimental or modeling techniques [39–42, 48–55], however here we are interested in retrieving the performance of the whole energy system.

We assume that the hydrogen has to be locally produced by NG coming from the distribution grid. However, we underline that the energy system in study could in principle operate on both H<sub>2</sub> (from water electrolysis) or natural gas, or a combination of the two [32]. Nowadays, it is necessary to develop efficient fuel processing plants in order to penetrate the market of distributed generation with FC technologies in the short medium term. Consequently, the CHP system can use existing infrastructure of NG, while being ready, and more competitive, for H<sub>2</sub> re-electrification, when renewable energy surplus makes H<sub>2</sub> generation a viable energy storage option [8, 56, 57].

Moreover, we underline that the technology of selective membranes can be used to process by steam reforming several fuels such as methanol, ethanol and glycerol [42, 49, 50, 53, 55], and also in other processes such as one step DME production process fed by CO<sub>2</sub> rich streams [40].

The paper is organized as follows. In section 2 the CHP system in study is presented. The numerical modeling methodology is accurately described in section 3. In section 4 the different fuel processing layouts analyzed are presented and characterized. Some in depth comparisons between the several case studies are presented in section 5. Finally, in section 6 we draw the conclusions of the work.

## 2. Problem Statement

The aim of this paper is to assess the impact of  $H_2$  selective membranes [37, 44] on the performance, cost, and system complexity reduction of the  $50\text{ kW}_{\text{el}}$  PEMFC based CHP plant, represented in Figure 1. Such a plant is connected to the NG line through a fuel processor based on SR, WGS, and syngas purification, that significantly impacts its performance.

### 2.1. Fuel Cell Based CHP Plant

We consider the  $50\text{ kW}_{\text{el}}$  CHP power plant represented in Figure 1. The prime mover is an automotive derivative low temperature PEMFC that converts hydrogen into electrical energy [32].

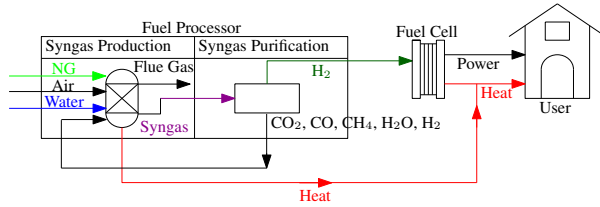


Figure 1: Schematic of the cogenerative PEM fuel cell system.

The low temperature PEMFC requires very high purity  $H_2$  (i.e. 99.999%, according to SAE J2719 [58]) that, in the near future, must be locally produced through a fuel processor (see Figure 1) because a diffused distribution grid for hydrogen is not present yet. A hydrogen rich syngas is obtained through NG steam reforming and WGS [37, 59]. Different technologies, including pressure swing adsorption separators and selective membranes [37], can be utilized to purify the syngas.

Fuel processing and purification strongly affect the overall performance of the considered energy system [38]. In fact, with a prime mover electrical efficiency in the range [45%, 55%] [22–24, 38], the resulting overall plant efficiency is between 32% and 38% [38] when utilizing a PSA. Such an efficiency is below the 42% target set by the FCH-JU [31].

We focus on the fuel processor technology. Specifically, we analyze the option of utilizing Pd-based selective membranes to separate pure  $H_2$  from reformat gas. We compare three configurations obtained by placing the membranes as separator device or integrating them in the WGS or SR reactors. The global efficiency is the principal performance parameter and is evaluated through the following equation:

$$\eta_{\text{glob}} = \frac{P_{\text{el}} - W_{\text{aux}}^{\text{ref}}}{\dot{m}_{\text{NG}} \text{LHV}_{\text{NG}}}, \quad (1)$$

where  $P_{\text{el}}$  is the FC net electrical power,  $W_{\text{aux}}^{\text{ref}}$  is the power required by the auxiliaries of the fuel processing section,  $\dot{m}_{\text{NG}}$  is the total natural gas mass flow entering in the energy system and  $\text{LHV}_{\text{NG}} = 46.5\text{ MJ/kg}$  is the lower heating value of the natural gas. Note that in the evaluation of the global efficiency (eq. (1)) the electric power output  $P_{\text{el}}$  is a net value, as evidenced in a previous work [38], already reduced of the power required by the auxiliaries of the FC plant (feeding air compressor and refrigerant circulation pumps). The fuel processor efficiency (eq. (2)) is also defined as:

$$\eta_{\text{fp}} = \frac{\dot{m}_{\text{H}_2} \text{LHV}_{\text{H}_2}}{\dot{m}_{\text{NG}} \text{LHV}_{\text{NG}}}. \quad (2)$$

where  $\dot{m}_{\text{H}_2}$  is the mass flow of  $H_2$  and  $\text{LHV}_{\text{H}_2} = 120\text{ MJ/kg}$  is its lower heating value. Moreover, the effect of auxiliaries can be considered also for the fuel processor efficiency leading to the expression reported in eq. (3).

$$\eta_{\text{fp}}^{\text{tot}} = \frac{\dot{m}_{\text{H}_2} \text{LHV}_{\text{H}_2} - W_{\text{aux}}^{\text{ref}}}{\dot{m}_{\text{NG}} \text{LHV}_{\text{NG}}}. \quad (3)$$

Finally, we evaluate the thermal efficiency as follows:

$$\eta_{\text{th}} = \frac{Q_{\text{cog}}}{\dot{m}_{\text{NG}} \text{LHV}_{\text{NG}}}, \quad (4)$$

where  $Q_{\text{cog}}$  is the thermal power available via cogeneration from the CHP plant.

The efficiencies are functions of the plant set-point, defined as:

$$\Phi = \frac{P_{\text{el}}}{P_{\text{el}}^{\text{nom}}}, \quad (5)$$

where  $P_{\text{el}}^{\text{nom}} = 50\text{ kW}_{\text{el}}$  is the maximum net electric power, and  $P_{\text{el}}$  is the net power output obtained by regulating the power plant.

### 2.2. Selective Membranes

Selective membranes, such as Pd-Ag alloys are a viable alternative to PSA [44]. Such membranes can reach efficiencies comparable or larger than PSA [44] and can operate at relatively high temperature ( $300^\circ\text{C}$ - $700^\circ\text{C}$ ) [60]. Thus, selective membranes at the state of the art can be integrated directly within the water gas shift and reforming reactor shifting chemical equilibrium towards larger hydrogen values. Membrane reactors have thus a potential in terms of plant simplification, in particular eliminating the necessity of syngas dehydration and the semi-batch PSA process. As a drawback, hydrogen is obtained at lower pressure (to ensure the driving force for separation), and thus hydrogen compression might be required after separation.

For application of selective membranes at low temperature (i.e. as simple separators) the stability can be guaranteed overcoming the phase change by alloying Pd with other metals such as Cu, Ag, and Au [60].

Different configurations, with respect to the integration of selective membranes within a reformer reactor are presented in literature [44], such as integrating the membranes directly in the steam reformer or in an autothermal reactor, or in the WGS reactor. The integration of the membranes in the steam reformer as well as the utilization of an autothermal reactor would require a substantial modification of the whole reforming plant.

### 3. Methodology

We perform the steady state modeling of the power plants introduced in section 2 using a lumped parameter approach. The simulation software is Aspen Plus<sup>®</sup> [61], integrated with proprietary Fortran codes. The modeling strategy is consistent with other studies found in literature [38, 44, 62, 63].

The main components of the analyzed power plants are: (i) Membrane Separator; (ii) Heat Integrated Wall Reactor (HIWAR); (iii) Membrane Integrated Reforming Reactor; (iv) Water Gas Shift Reactor; (v) Membrane Integrated Water Gas Shift Reactor; (vi) Heat Exchangers; (vii) Auxiliaries; (viii) Automotive Derivative Fuel Cell; (ix) PSA Separator.

In the modeling environment we use the Peng Robinson equation [61] of state to compute the thermodynamic properties of working fluids. In addition, for pure water streams, the steamNBS tables are used [64].

#### 3.1. Membrane Separator

The conceptual scheme for a membrane separator is shown in Figure 2. H<sub>2</sub> permeation through a Pd mem-

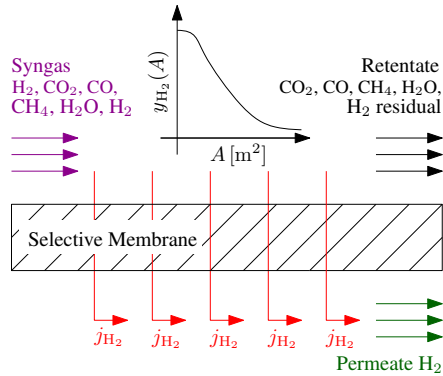


Figure 2: Membrane separator scheme and nomenclature.

brane is described by the well-known Sieverts' law [65], which is expressed by eq. (6), in the case that H<sub>2</sub> diffusion through the bulk of Pd membrane is rate-limiting, i.e. the H<sub>2</sub> flux is proportional to the square root of the H<sub>2</sub> partial pressure difference ( $n = 0.5$ ).

$$j_{H_2} = K_{H_2} \left( p_{H_2,ret}^n - p_{H_2,perm}^n \right), \quad (6)$$

where  $K_{H_2}$  is the hydrogen permeance of the membrane,  $p_{H_2,ret}$  and  $p_{H_2,perm}$  are the H<sub>2</sub> partial pressure on the retentate and permeate sides of the membrane, respectively. Deviations from Sieverts' law behavior (i.e.  $n > 0.5$ ) have been attributed to various factors including surface and gas diffusion limitations, and have been used in literature to investigate the rate-controlling step of the permeation of H<sub>2</sub> through a Pd-based membrane. The main factors determining the hydrogen permeance are the thickness of the membrane selective layer and the temperature [66]. State of the art membranes reach permeance values around  $10^{-2} \text{ mol}/(\text{m}^2 \text{ s Pa}^{0.5})$  at 350 – 400 °C, thereby reaching values higher than the 2015 target set by the U.S. DoE ( $8.5 \times 10^{-3} \text{ mol}/(\text{m}^2 \text{ s Pa}^{0.5})$ ) [67]. However, these values are obtained in pure H<sub>2</sub> as feed gas where there are no surface and gas diffusion limitations for transport. Measurements obtained under real operating conditions have shown that the permeance can be decreased by roughly a factor of 5 compared to a situation where pure H<sub>2</sub> is applied as feed. In the current modelling study, we have therefore investigated the membrane performance assuming a permeance value of  $8.5 \times 10^{-3} \text{ mol}/(\text{m}^2 \text{ s Pa}^{0.5})$ , which is the DoE target, and a permeance value one order of magnitude lower ( $8.5 \times 10^{-4} \text{ mol}/(\text{m}^2 \text{ s Pa}^{0.5})$ ).

Referring to eq. (6), the driving force vanishes when  $p_{H_2,ret} = p_{H_2,perm}$ . Note that we assume the absence of a sweep flow in the permeate side to have a better performing FC [46]. Thereafter, the minimum hydrogen concentration possible in the retentate is  $y_{H_2}^{\min} = p_{perm}/p_{ret}$  and can be reached only by using an infinite surface membrane.

The following equation evaluates the H<sub>2</sub> concentration in the retentate as a function of the membrane area  $A$  ( $y_{H_2}(A)$ ):

$$y_{H_2}(A) = \frac{n_{H_2,syn} - \int_0^A j_{H_2}(A) dA}{n_{tot}(A)}, \quad (7)$$

where  $n_{H_2,syn}$  is the initial number of H<sub>2</sub> moles in the syngas and  $n_{tot}(A)$  is the total number of moles in the retentate. Equation (7) is numerically integrated using the Euler method to obtain  $y_{H_2}(A)$  shown in Figure 3. Therein, we consider the following retentate and the

permeate total pressures,  $p_{\text{ret}} = 11.5$  bar and  $p_{\text{perm}} = 1.20$  bar, respectively. The initial syngas mole flow is  $\dot{f}_{\text{H}_2}^{\text{syn}} = 0.944$  mol/s, carrying a hydrogen mole flow  $\dot{f}_{\text{H}_2}^{\text{syn}} = 0.482$  mol/s. The selectivity of the membrane is assumed to be infinite, and hydrogen is separated. For the integration of eq.(7), we assume  $dA = 10^{-3}$  m<sup>2</sup> after a convergence analysis on the total pure hydrogen flux  $J_{\text{H}_2}$ . Figure 3 evidences that  $K_{\text{H}_2}$  influences the area required for the separation, but not  $y_{\text{H}_2}^{\text{min}}$ , or in other words the separation efficiency.

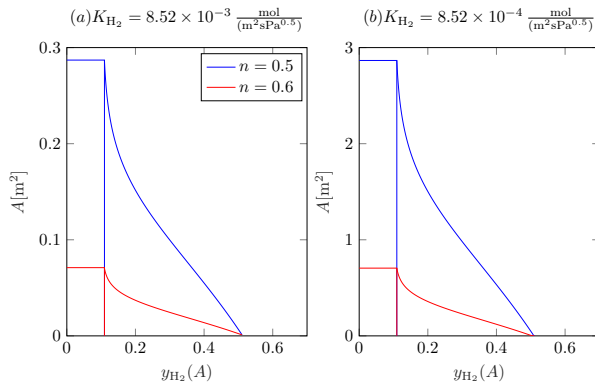


Figure 3: Variation of the surface of the membrane separator with respect to the hydrogen concentration in the retentate, as a function of the driving force exponent in two different cases: a)  $K_{\text{H}_2} = 8.52 \times 10^{-3}$  mol / (m<sup>2</sup>sPa<sup>0.5</sup>); b)  $K_{\text{H}_2} = 8.52 \times 10^{-4}$  mol / (m<sup>2</sup>sPa<sup>0.5</sup>).

For  $y_{\text{H}_2} \geq 0.2$  (i.e.  $y_{\text{H}_2} \geq 1.92y_{\text{H}_2}^{\text{min}}$ ) the membrane area increases linearly by reducing the H<sub>2</sub> concentration (see Figure 3). Conversely, a further reduction of  $y_{\text{H}_2}$  causes a sharp increment of the required surface. Thus, in the followings, we assume that the H<sub>2</sub> concentration at the exit of the membrane separator is  $y_{\text{H}_2} = 1.05y_{\text{H}_2}^{\text{min}}$  and we denote  $J_{\text{H}_2} = \int_0^A j_{\text{H}_2}(A) dA$ . The separation efficiency (also known as hydrogen recovery factor) is defined as:

$$\eta^{\text{SEP}} = \frac{J_{\text{H}_2}}{\dot{f}_{\text{H}_2}^{\text{syn}}}. \quad (8)$$

The retentate pressure largely determines  $\eta^{\text{SEP}}$  through its influence on  $y_{\text{H}_2}^{\text{min}}$ , as evidenced in Figure 4. Specifically,  $\eta^{\text{SEP}}$  increases from 2.65 % to 89.3 % varying  $p_{\text{ret}}$  from 2.50 bar to 12.5 bar. On the contrary it further increments just to 94.3 % increasing  $p_{\text{ret}}$  to 22.5 bar.

### 3.2. HIWAR

Steam reforming is performed in the HIWAR [68, 69], where the catalytic oxidation of natural gas and

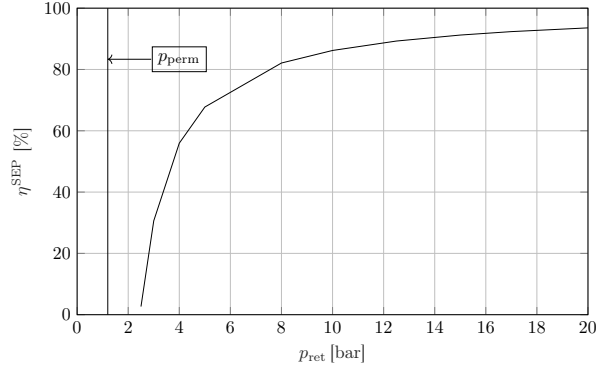


Figure 4: Maximum attainable separation efficiency of Pd-based selective membranes as a function of the feed pressure, for  $p_{\text{perm}} = 1.20$  bar,  $\dot{f}_{\text{ret}} = 0.944$  mol/s,  $\dot{f}_{\text{H}_2}^{\text{ret}} = 0.482$  mol/s, and  $y_{\text{H}_2} = 1.05y_{\text{H}_2}^{\text{min}}$ .

the steam reforming reactions take place in a single element. Such a device is a ceramic tube coated with a metal catalyst film, specific for the oxydation, in its inner side and with another catalytic substance, specific for the reforming, in the outer. The heat flux between the two sides of the reactor is allowed by the conductive wall.

In our model such a component is simulated through two separate reactors. The coupling of the elements, i.e. the heat integration, is then implemented through an heat flux from the burner to the reformer (Figure 5).

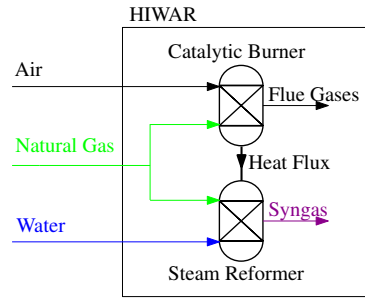
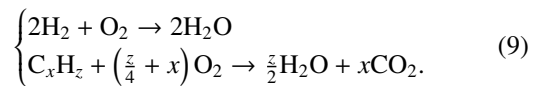


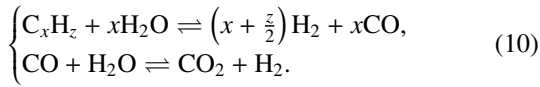
Figure 5: Schematic overview of the HIWAR reactor model.

The temperature of the catalytic burner is 845 °C. Thus a common equilibrium reactor would be not effective. Therefore, we use the stoichiometric reactor (RStoic in Aspen Plus®) and specify the chemical reactions that take place and the associated fractional conversion. The following equation reports the reactions implemented for the catalytic burner reactor:



The fractional conversion of each oxidized element is set to 100%.

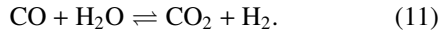
The steam reforming is modeled as an equilibrium reactor (called RGibbs in the modeling environment). Aspen Plus<sup>®</sup> calculates the equilibrium composition of the resulting flows minimizing the Gibbs free energy [61]. The temperature and pressure of the reactor will determine the prevailing reactions through the equilibrium constants. The reforming side of the HIWAR reactor is operated at a temperature of 770 °C. The following equation, reports the dominant reactions at such a temperature:



Note that at 770 °C, the chemical reaction equilibrium constants for methane (the main component of NG) steam reforming and water gas shift are  $K_{REF} = 84.4$  and  $K_{WGS} = 1.21$  [70] respectively. The NG steam reforming is the largely predominant reaction, being  $K_{REF} \cong 70 \times K_{WGS}$ .

### 3.3. Water Gas Shift Reactor

The water gas shift reaction is conventionally applied in fuel processing plants, to produce further hydrogen from carbon monoxide and water, as follows:



We utilize the stoichiometric equilibrium reactor that allows the user to specify the stoichiometry of the reactions that has to be simulated (in this case the reaction reported in eq. (11)). Such a modeling choice is required to exclude the steam reforming reaction from chemical equilibrium computations. The reforming reaction besides having a lower equilibrium constant compared to reaction (11) is also kinetically hindered: at 320 °C, the chemical reaction equilibrium constants for water gas shift and methane steam reforming are  $K_{WGS} = 24.9$  and  $K_{REF} = 2.32 \times 10^{-7}$  [70] respectively, and this reactor utilizes specific catalysts to promote reaction (11) rather than steam reforming. For these reasons, the water gas shift is largely predominant.

### 3.4. Membrane Reforming and Water Gas Shift Reactors

Pd-based selective membranes resist to relatively high temperatures and pressures and thus can be integrated directly in reactors (Figure 6). In this way the hydrogen produced is separated from the reactants, shifting the reaction towards products. The integration can

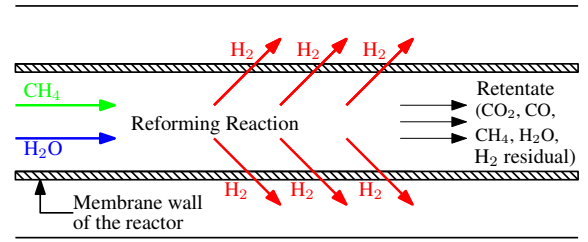


Figure 6: Schematic overview of membrane reactors.

be performed both in the water gas shift and in the reforming reactors.

For these processes we have developed a 1-D reactor model in Aspen Plus<sup>®</sup>, that is an inherently 0-D simulation environment. To this aim, we discretize the membrane reforming and membrane WGS as a sequence of reactors and separators, as shown in Figure 7.

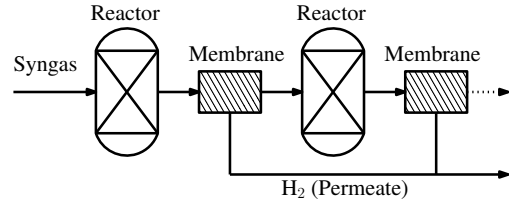


Figure 7: Modeling approach used for the membrane reactors.

To determine the most appropriate number of discretization steps a convergence analysis is performed. Specifically, the mass flow of the pure hydrogen produced by the fuel processing plant is considered as the convergence parameter. We verified that the H<sub>2</sub> flow varies less than a 1% by incrementing the number of discretization steps from five to six, for both reforming and water gas shift reactor. Therefore, 6 steps are used for the discretization of all membrane reactors.

### 3.5. Heat Exchangers

All heat exchangers are studied through the logarithmic mean temperature difference model. An accurate modeling of the off-design performance is considered, since the thermal resistance varies as a function of the hydrogen mass flow rate. In design conditions the product between the heat exchange coefficient and the area of the heat exchanger is calculated as [71]:

$$\Gamma^* = \frac{Q}{\Delta T_{ml}}, \quad (12)$$

where  $Q$  is the thermal power and  $\Delta T_{\text{ml}}$  the logarithmic mean temperature difference.

When mass flows change, the product  $UA$  is calculated as:

$$\Gamma = \Gamma^* \left( \frac{\dot{m}}{\dot{m}^*} \right)^{0.8}, \quad (13)$$

where  $\dot{m}$  and  $\dot{m}^*$  are the mass flows in off-design and design conditions respectively.

When  $\dot{m} \neq \dot{m}^*$  for both the hot and the cold side of the heat exchanger, the mass flow with the lower heat transfer coefficient is considered in eq. (13).

In several heat exchangers, the heat capacity of one or both the flows varies due to condensation or evaporation. In such cases, a single heat exchanger is subdivided into several elements and the number of discretization steps is determined through a convergence analysis. The output enthalpy of hot and cold streams is selected as convergence parameter. The most critical case (i.e. HE-5 in Figure 17) converges for 10 discretization steps. Thus all the heat exchangers are subdivided into 10 elements.

### 3.6. Auxiliaries

Several fluid machineries provide the required pressure to the fluids in each plant section. Specifically, there are: (i) a natural gas compressor, (ii) a water pump for the high pressure steam generation, (iii) an air compressors for circulation, (iv) an air compressor for the fuel cell, (v) two water pumps for circulation in the fuel cell balance of plant and, in some cases, (vi) an hydrogen compressor.

The power required from the auxiliaries, is evaluated as:

$$W_{\text{aux}} = \eta^{\text{is}} (h^{\text{out}} - h^{\text{in}}), \quad (14)$$

where  $h$  is the enthalpy of the fluid calculated from the Peng Robinson equation [61] of state and  $\eta^{\text{is}}$  is the isentropic efficiency of the pump/compressor. Values for the efficiency of the devices are retrieved from an Aspen Plus library of real machines.

### 3.7. Automotive Derivative Fuel Cell

The main components of the fuel cell model are (Figure 8): (i) the PEMFC stack, (ii) the air compressor, (iii) two cooling circuit with different temperature levels, (iv) two pumps for water circulation, (v) two heat exchanger for co-generation. In the model a control system is also simulated, in order to maintain the proper ratio between air and hydrogen mass flows.

The cathodic exhaust and the high temperature coolant circuit stream of the fuel cell are exploited for co-generation purposes.

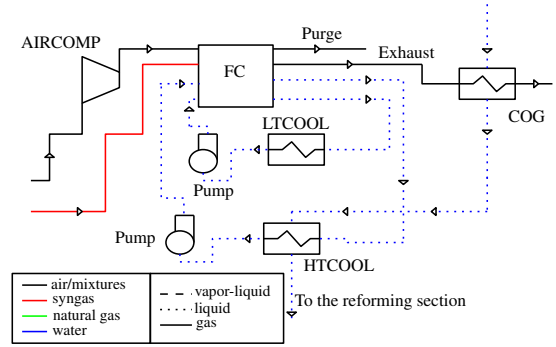


Figure 8: Schematic representation of the model implemented for the fuel cell.

The model of the PEMFC stack relies on experimental data of the automotive FC provided by NuCell-Sys and reported in Figure 9. Specifically the black-box model calculates the electric power as a function of the input hydrogen mass flow rate. It also returns the thermo-physical properties, compositions, and mass flow rates of air, purge, exhaust, and coolants mass flows.

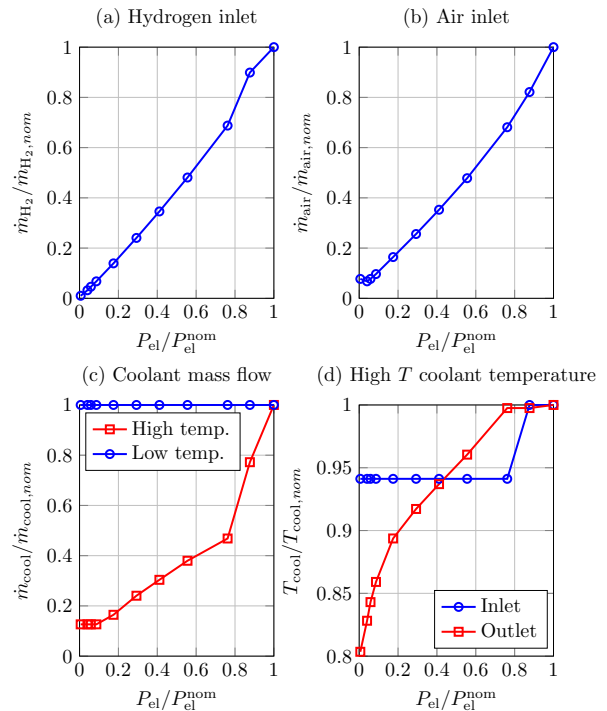


Figure 9: Experimental performance of the automotive derivative PEMFC system. Data are reported in a non-dimensional form.

Note that in Figure 9(d) each temperature profile is normalized with respect to its nominal value. As a con-



sequence, despite normalized inlet temperature is lower than normalized outlet, the physical values are coherent (i.e. outlet lower than inlet).

### 3.8. Pressure Swing Adsorption Separator

The PSA is modeled with a black box phenomenological approach. The utilized experimental data are reported in Figure 10. The separation efficiency varies

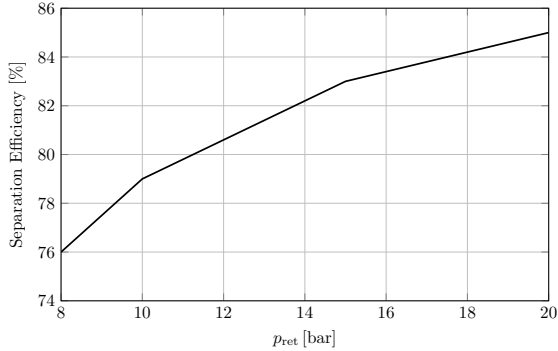


Figure 10: Experimental data for the pressure swing adsorption separator: separation efficiency is expressed as a function of the feed pressure.

between 76% and 85%, respectively at 8 bar and 20 bar syngas feed pressure,  $p_{ret}$ .

The black-box model calculates composition, mass flow rate and pressure of the pure hydrogen and retentate flows, taking as input such characteristics of the syngas.

## 4. Case Studies

Table 1 summarizes the considered power plant configurations. Note that each plant has a different natural gas mass flow rate to obtain the same  $H_2$  mass flow rate entering the FC. In this way, the comparison is not biased by the FC efficiency, which is a function of its  $H_2$  input mass flow rate, or equivalently of the set-point, as evidenced in Figure 9.

### 4.1. Plant A: Baseline Plant

Plant A, schematically reported in Figure 11, is the baseline configuration.

At  $\Phi = 1$ , 10.4 kg/h of NG are compressed to 12 bar and mixed with 38.7 kg/h of super-heated steam at a temperature of 457 °C. The ratio between the mass flow rates of the NG and of the steam entering the reformer is fixed to  $\psi = 3.73$ . The resulting mixture, at a temperature of 399 °C, is further heated in HE-3 to 760 °C. Such a temperature is the minimum possible to avoid

Table 1: Summary of the considered fuel processor configurations.

Case	Description	$\dot{m}_{NG}^{REF} + \dot{m}_{NG}^{BURN}$ [kg/h]
Plant A	Steam reforming, water gas shift, purification via PSA	10.4+0.204
Plant B	Steam reforming, water gas shift, purification via selective membranes	9.45+0.886
Plant C	Steam reforming, membrane integrated water gas shift	9.21+0.868
Plant D	Membrane integrated steam reforming	6.90+2.62

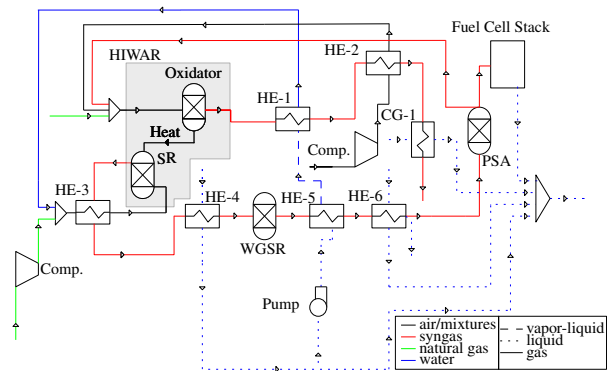


Figure 11: Schematic overview of the baseline energy conversion plant.

an efficiency drop of the reaction [24, 72]. In the same heat exchanger the syngas temperature is reduced from 770 °C to 436 °C. The working pressure is imposed as a trade-off between the reaction performance [43, 59] and the PSA efficiency (see Figure 10).

In HE-4 the syngas is further cooled to 320 °C, in order to have a favorable water gas shift reaction kinetics. The thermal power extracted from the hydrogen rich gas in HE-4 is used for co-generation. The syngas exits the WGSR at 381 °C, being the CO shift an exothermic reaction. The thermal energy still present in the  $H_2$  rich gas is used both to pre-heat the water necessary for the reforming reaction and for co-generation purposes. Specifically, in HE-5 the water is heated from 15.0 °C to 188 °C with a vapour fraction of 0.25, while the syngas is cooled to 128 °C.

The hydrogen rich gas is further cooled to 50 °C for

co-generation purposes in HE-6. The gas mixture is then purified in the PSA section and a flux of pure hydrogen is separated to be used in the fuel cell. The rest of the syngas is used in the burner side of the HIWAR reactor (see section 3.2) together with air and natural gas.

The combustion reaction occurs at 845 °C and at ambient pressure and 0.204 kg/h of NG are burned in the oxidator to guarantee the thermal equilibrium of the HIWAR. The total NG mass flow rate is 10.6 kg/h (see Table 1) yielding 3.09 kg/h of pure H<sub>2</sub>, that generates 50 kW<sub>el</sub> of net electrical power in the FC. In HE-1 the mixture of water and steam exiting HE-5 is heated at 457 °C and the flue gases are cooled down from 845 °C to 198 °C. Subsequently in HE-2 the combustion products are further cooled to 101 °C. As a consequence, the air temperature rises to 188 °C. Finally flue gases are left to the environment at 75 °C after a co-generative heat recovery.

The mass flow rate of the hot water produced in CG-1, HE-6 and HE-4 is determined such that its temperature  $T_{\text{COG}} = 99$  °C. The resulting overall hot water mass flow rate is 246 kg/h. Thereof, the cogenerated power is 82.5 kW<sub>th</sub>, including 68.3 kW<sub>th</sub> from the fuel cell.

Concentrated pressure drops are considered in several elements of the fuel processing plant. Specifically, the pressure drop is reduced by: (i) 0.100 bar in the reformer, (ii) 0.050 bar in both hot and cold side of HE-3, (iii) 0.010 bar in HE-4, (iv) 0.250 bar in the water gas shift reactor, (v) 0.030 bar in HE-1, HE-5 and HE-6, (vi) 0.020 bar in HE-2.

We underline that such a CHP power plant has been already studied in a previous work of the authors [38], however in this case we refine the thermal integration of the components and we implement the accurate modeling approach for heat exchangers described in section 3.5.

We determine the part load efficiency of plant A by reducing  $\dot{m}_{\text{NG}}^{\text{ref}}$  to 5.19 kg/h. A further reduction is hindered by the PSA. Figure 12 reports  $\eta_{\text{glob}}$  and  $\eta_{\text{th}}$  as function of  $\Phi$ .

The overall electrical efficiency varies between 35.0% and 40.0%, as a function of  $\Phi$ , being higher at part load. This is a typical feature of CHP plants based on fuel cells [22–24, 38]. Such a behavior is dominated by the efficiency curve of the FC [22–24, 38].

The shadowed region in the plot (Figure 12(a)) is obtained considering two limit cases. For the upper curve, NG comes from the distribution grid already at the working pressure of 12 bar. For the lower curve, the natural gas is distributed at 1 bar and has to be compressed to 12 bar within the power plant. In real cases

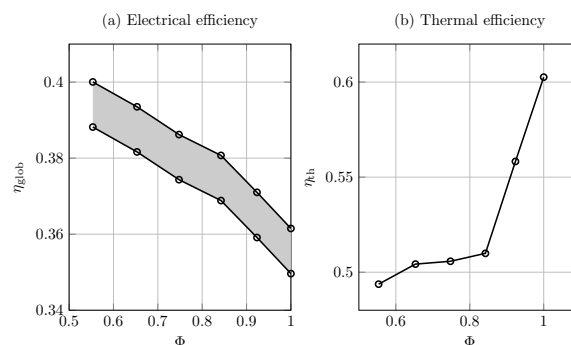


Figure 12: Efficiency of the baseline power plant (Plant A) as a function of  $\Phi$ : (a) overall electrical efficiency; (b) thermal efficiency. The shaded band between the two lines in graph (a) identifies the performance with and without including the work needed to compress the natural gas at the fuel processor inlet.

NG will be delivered with a pressure between 1 bar and 12 bar, and the real efficiency will be somewhere in the shadowed area. The efficiency difference between the upper and the lower curve is always 1.19 %.

The presence of auxiliary elements has a huge impact on the CHP efficiency. Specifically, in design conditions, the energy consumption of the natural gas compressor and of the other auxiliaries of the fuel processing plant are respectively 3.24 % and 1.43 % of the nominal fuel cell electric power.

Thermal efficiency (see Figure 12 (b)) varies between 49.4% and 60.2%. The higher  $\Phi$ , the higher is  $\eta_{\text{th}}$ , as a consequence of the fuel cell performance variation from part to full load operations. The rapid change in slope of the thermal efficiency curve at  $\Phi = 84.2$  % is probably due to the increasing relevance of the gas transport losses [22–24]. Such a statement is validated also looking at the sudden increment in the coolant mass flow rate for  $\Phi > 80.0$  % shown in Figure 9.

#### 4.2. Plant B: Membrane Separator

Plant B is schematically depicted in Figure 13.

The fuel processing plant is similar to Plant A (see section 4.1). The main difference is that the PSA is replaced by a selective membrane. The membrane unit in Figure 13 is modeled according to the approach described in section 3.1. Pure H<sub>2</sub> is released at 1.20 bar and compressed to 2.00 bar to be utilized in the fuel cell. The required membrane area to obtain  $y_{\text{H}_2} = 1.05 y_{\text{H}_2}^{\text{min}}$  in nominal conditions and considering  $K_{\text{H}_2} = 8.5 \times 10^{-3} \text{ mol}/(\text{m}^2 \text{ s Pa}^{0.5})$  is  $A_{\text{memb}}^{\text{SEP}} = 0.286 \text{ m}^2$ . The resulting separation efficiency of the membrane is 80.3 %.

The working pressure of the reformer is kept to 12 bar. Thus, the reaction performance is not significantly

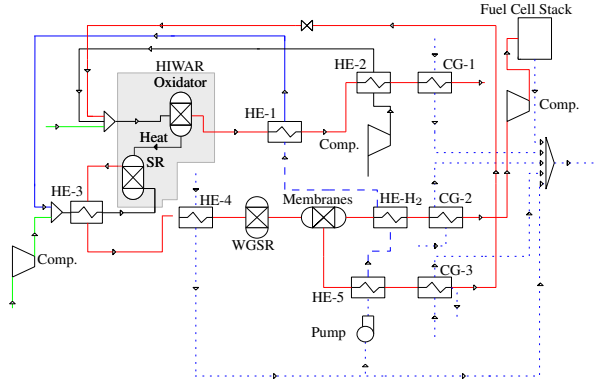


Figure 13: Schematic overview of the energy conversion plant with a membrane separator.

varied [43, 59], while the membrane efficiency (maintaining permeate conditions at 1.20 bar) is similar to the PSA ones (see section 4.2, specifically Figure 4).

In this plant configuration, the hydrogen production system is more efficient than in Plant A. In fact, in Plant B it is possible to produce the same mass flow of hydrogen, using 9.13 % less natural gas in the reformer. However in the last case the NG mass flow rate required in the burner is 4.34 times the amount registered in Plant A case. This is due to the lower amount of hydrogen in the retentate, that requires to integrate the overall thermal balance with additional chemical energy.

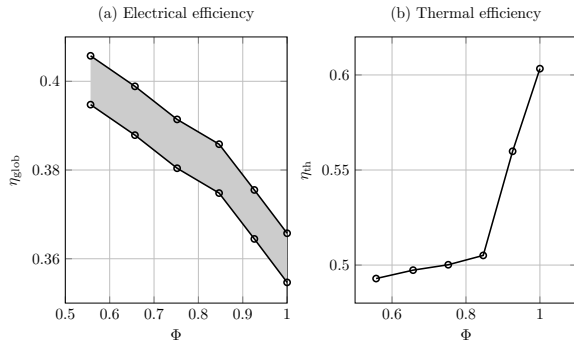


Figure 14: Efficiency of the membrane separator power plant (Plant B) as a function of  $\Phi$ : (a) overall electrical efficiency; (b) thermal efficiency. The shaded band between the two lines in graph (a) identifies the performance with and without including the work needed to compress the natural gas at the fuel processor inlet.

The overall electrical efficiency varies between 35.5 % and 40.5 %, while  $49.3\% < \eta_{th} < 59.8\%$ , as evidence in Figure 14.

The impact of the auxiliaries is pivotal also in this case. In fact, the energy consumption of the natural gas compressor and of the other auxiliaries of the fuel

processing plant are 2.95 % and 1.30 % of  $P_{el}^{nom}$ , respectively. Note that also the  $H_2$  compressor has a relevant impact on  $\eta_{glob}$ . In fact, its power consumption is 1.38 % of  $P_{el}^{nom}$ .

#### 4.3. Plant C: Water Gas Shift Membrane Reactor

The water gas shift membrane reactor power plant is reported (Figure 15).

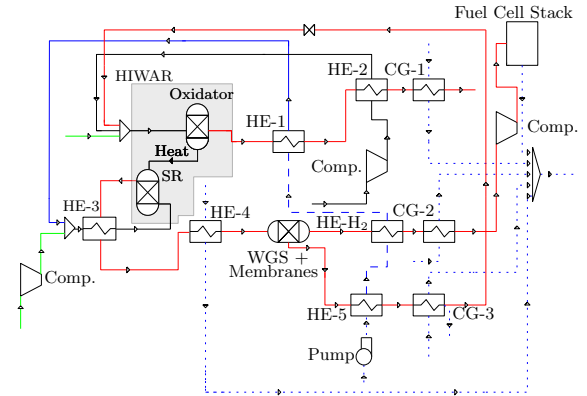


Figure 15: Schematic overview of the energy conversion plant with a water gas shift membrane reactor.

In this configuration hydrogen purification takes place directly in the water gas shift reactor. Thus, the purification section downstream is not necessary anymore, leading to a significant plant simplification. The membrane separator integration in the WGS reactor is performed following the approach illustrated in section 3.4.

The water required by the steam reforming is first preheated in HE-5, reducing the retentate gas temperature, and then in HE-H<sub>2</sub> reducing the temperature of the pure H<sub>2</sub>. Similarly, the water of the co-generation circuit first exchanges heat with retentate gases (CG-2) and then with pure H<sub>2</sub> (CG-3).

The WGS reactor is operated at 12 bar, which is the optimal trade off between hydrogen separation and auxiliaries work [43].

The membrane surface necessary to achieve  $y_{H_2} = 1.05y_{H_2}^{min}$  is  $A_{memb}^{WGS} = 0.260 \text{ m}^2$ , considering  $K_{H_2} = 8.5 \times 10^{-3} \text{ mol}/(\text{m}^2 \text{ s Pa}^{0.5})$ . The resulting  $\dot{m}_{H_2}$  is 99.0 % of the one obtainable with an infinite surface reactor, given the initial syngas conditions.

In this case 10.1 kg/h of NG are required to obtain 50 kW<sub>el</sub> of nominal net electrical power from the FC, or, equivalently, 3.09 kg/h of pure H<sub>2</sub>. Membranes shift the equilibrium of reaction (10) towards H<sub>2</sub>. Thereafter, the CO concentration in the tail gases is 0.498 %.

Such a value is considerably lower compared to Case A (3.20 %) and B (2.90 %).

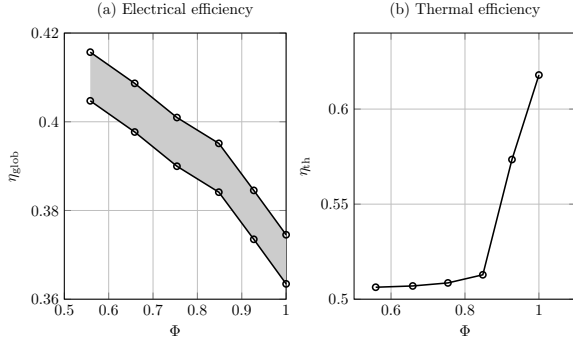


Figure 16: Efficiency of the water gas shift membrane reactor power plant (Plant C) as a function of  $\Phi$ : (a) overall electrical efficiency; (b) thermal efficiency. The shaded band between the two lines in graph (a) identifies the performance with and without including the work needed to compress the natural gas at the fuel processor inlet.

The global electrical efficiency varies between a minimum of 36.3% and a maximum of 41.6%, as evidenced in Figure 16.

The thermal efficiency (see Figure 16 (b)) is comprised between 50.6% and 61.8%.

#### 4.4. Plant D: Reforming Membrane Reactor

Figure 17 represents configuration D. In this case,

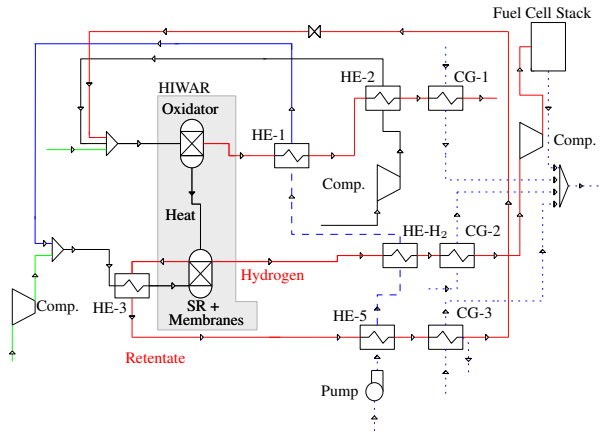


Figure 17: Schematic overview of the energy conversion plant with a reforming membrane reactor.

the membranes are integrated directly in the steam reforming side of the HIWAR reactor, making the water gas shift reactor unnecessary. Note that only  $H_2$  is drained by the membrane shifting the equilibrium of reaction (10)(b) towards the products. As a consequence

the CO mass flow rate in the retentate is just 1.68 % of the total pure hydrogen produced, much lower than 3.20 % and 2.94 % observed for plants A and B, respectively. On the contrary, the CO concentration in the retentate is higher than that observed for plant C due to the lower temperature of the shift reactor, compared to the reformer.

Note that the membrane separator integration in the steam reforming reactor is performed according to the approach illustrated in section 3.4.

The working pressure of the reformer is set to 35 bar. Such an assumption is justified by the sensitivity analysis reported in section 5.1.

The surface of the selective membrane required to obtain  $y_{H_2} = 1.05y_{H_2}^{min}$  is  $A_{memb}^{REF} = 0.250 m^2$ , considering  $K_{H_2} = 8.5 \times 10^{-3} mol / (m^2 s Pa^{0.5})$ . We use here the same permeance value of the other plant configurations. However, the relatively high temperature of the reformer reactor (i.e.  $770^\circ C$ ) would result in a higher  $K_{H_2}$  and, as a consequence, a lower membrane surface for the same performance. Such aspect would lower the cost of the energy system, that here is not investigated in detail.

The range of the possible set-points in cases A, B, C is limited around 60.0% by PSA and reformer constraints of the real fuel processing plant under construction within the European project [32]. However, in this case the fuel converter is completely different in the construction, so we cannot determine a priori the minimum possible set-point. For this reason the sensitivity analysis is performed for a wider operating range (see Figure 18). The value of the natural gas mass flow rate entering the power plant, in design conditions, is, in this case,  $\dot{m}_{NG}^{REF} + \dot{m}_{NG}^{BURN} = 9.52 kg/h$ .

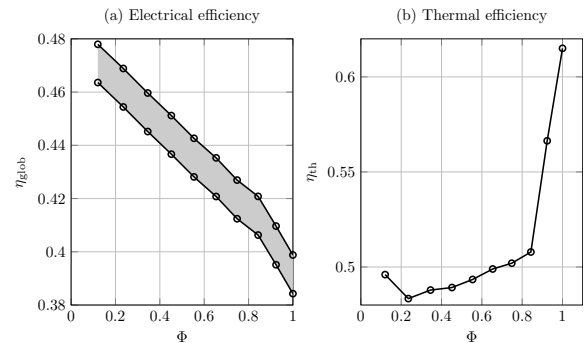


Figure 18: Efficiency of the reforming membrane reactor power plant (Plant D) as a function of  $\Phi$ : (a) overall electrical efficiency; (b) thermal efficiency. The shaded band between the two lines in graph (a) identifies the performance with and without including the work needed to compress the natural gas at the fuel processor inlet.

The global electric efficiency of the power plant varies between 38.4% and 47.8%, being the highest of all analyzed configurations, as represented in Figure 18(a).

The thermal efficiency increases by increasing  $\Phi$  as evidenced in Figure 18(b), mainly because the FC operation is less efficient (degradating more chemical energy into heat). In particular,  $\eta_{th}$  varies in the range [49.6%, 61.5%]. The sharp change of slope for set-points  $\Phi < 12.0\%$  is probably due to the fuel processor efficiency drop in such a region (see Figure 19(a)).

## 5. Discussion

A comparison between the results obtained in all the configurations previously presented is now performed. The efficiency values for each power plant, for  $\Phi = 1$ , are reported in table 2.

Table 2: Efficiency values in nominal conditions for each power plant analyzed.

Case	$\eta_{fp}$ [%]	$\eta_{glob}$ [%]	$\eta_{th}$ [%]
Plant A	75.1	35.0	60.3
Plant B	77.0	35.5	60.3
Plant C	78.7	36.3	61.8
Plant D	83.8	38.4	61.5

Figure 19 reports the relevant performance of the power plant as functions of the set-point.

The fuel processor efficiency has almost a flat response to the load condition. The average values are  $\eta_{fp} = 75.1\%$ ,  $\eta_{fp} = 77.0\%$ ,  $\eta_{fp} = 78.8\%$ ,  $\eta_{fp} = 83.7\%$ , respectively for Plant A, B, C and D. Rearranging eqs. (1), and (2) and defining the fuel cell efficiency as:

$$\eta_{FC} = \frac{P_{el}}{\dot{m}_{H_2} LHV_{H_2}}, \quad (15)$$

we can write the following equation for the fuel processor efficiency:

$$\eta_{fp} = \frac{\eta_{glob}}{\eta_{FC}} + \frac{W_{aux}^{ref}}{\dot{m}_{NG} LHV_{NG} \eta_{FC}}. \quad (16)$$

Considering the target  $\eta_{glob} = 0.420$ , and a mean  $\eta_{FC} = 0.500$  and  $W_{aux}^{ref}/\dot{m}_{NG} LHV_{NG} = 0.0191$  we get  $\eta_{fp} = 0.878$ . Such an efficiency of the fuel processor should be reached in nominal conditions to attend the FCH-JU [31] goal.

The most relevant parameter is  $\eta_{glob}$  that, at nominal conditions, increases by 9.71% (i.e. from 35.0% to

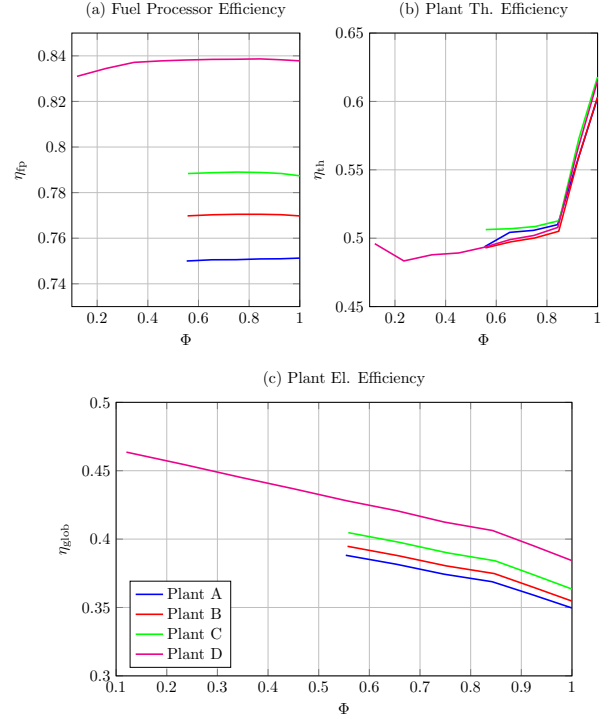


Figure 19: Performance of the considered power plants as functions of  $\Phi$ : (a) fuel processor efficiency; (b) plant thermal efficiency; (c) plant minimum electric efficiency (natural gas from the grid at 1 bar).

38.4%) switching from Plant A to Plant D. This is possible mainly for two reasons: (i) shift of the reforming reaction towards products; (ii) better thermal integration for heat recovery in the reacting fluxes. The target for the overall plant electric efficiency set by the FCH-JU [31] is 42.0%, Plant D configuration meets such a prescription for  $\Phi < 65\%$ . However, in a real energy management scenario, the plant set-point will rarely be 1, making the effective electrical efficiency supposedly higher than the target. Moreover, configurations aiming at increasing the energy converter efficiency can be adopted, like for example the usage of two fuel cells of nominal power  $50 \text{ kW}_{el}$  in parallel downstream the fuel processor to improve the FC electrical efficiency [38].

We note that configurations B and C significantly reduce the fuel processor complexity with respect to the baseline configuration A by eliminating the semi-batch PSA process. However, their impact on the system efficiency is minor compared to configuration D.

In fact, only the integration of the membrane within the HIWAR promotes an effective shift of the equilibrium reactions towards  $H_2$  production. Moreover, it significantly improves the thermal integration of the fuel processor components by avoiding the cooling process

to 320° C, necessary for water gas shift reaction, before thermal recovery.

Thereafter, in the following sections we further dissect the power plant D by systematically varying the important operating parameters (i.e. pressure, applied membrane surface, reformer temperature and pinch point of the heat exchangers). The aim is to establish the most convenient working parameters, considering thermodynamic performance as well as technological and economic aspects.

### 5.1. Effects of the Reformer Pressure and of the Membrane Surface

We study the effect of the reformer pressure, in order to establish the optimal operating conditions for configuration D. In fact, literature data are available for the simple reforming reaction [43, 59]. The presence of hydrogen separation through selective membranes, that is a function of the pressure gradient, might change the optimal operating conditions. In addition a sensitivity analysis to the applied membrane surface area is performed. Results for  $\dot{m}_{\text{NG}}^{\text{REF}} = 6.90 \text{ kg/h}$ , and considering  $K_{\text{H}_2} = 8.5 \times 10^{-3} \text{ mol}/(\text{m}^2 \text{ s Pa}^{0.5})$ , are reported in Figure 20. The power required from the auxiliaries is evaluated assuming the natural gas coming from the grid at 1 bar

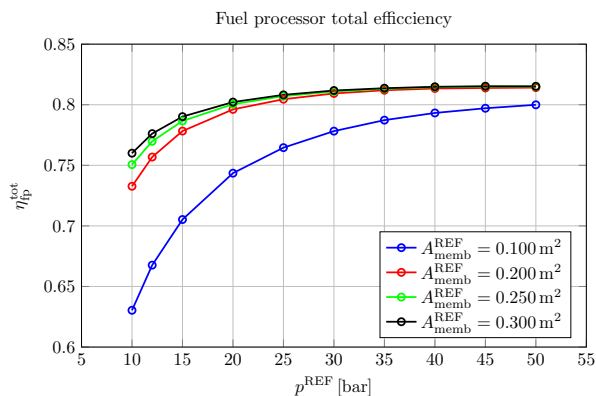


Figure 20: Fuel processor efficiency as a function of the pressure  $p^{\text{REF}}$ , and of the applied membrane surface area  $A_{\text{memb}}^{\text{REF}}$ . The power required from the auxiliaries is evaluated considering the natural gas coming from the grid at 1 bar.

We note, from Figure 20, that  $\eta_{\text{fp}}^{\text{tot}}$  varies in the range [63.0 %-81.5 %], as a function of the reformer pressure and of the applied membrane surface area. In fact, the fuel processor total efficiency increases augmenting such parameters. However, we also note a saturation in the performance increase. We consider in this analysis the fuel processor total efficiency  $\eta_{\text{fp}}^{\text{tot}}$ , defined in eq (3), in order to take into account the effects of the pressure

rise in the work required by the auxiliaries. Summarizing,  $A_{\text{memb}}^{\text{REF}} = 0.250 \text{ m}^2$  and  $p^{\text{REF}} = 35.0 \text{ bar}$  should be considered as a techno-economic compromise. In fact, decreasing these two values results in a decrement of the performance. On the other hand, further increasing them is unnecessary because the efficiency improvement would be marginal and would not compensate the higher cost of the overall energy plant.

For  $p^{\text{REF}} > 30 \text{ bar}$  and  $A_{\text{memb}}^{\text{REF}} \geq 0.200 \text{ m}^2$  the efficiency curves collapse. Nevertheless, Figure 20 evidences that, when the membrane surface is too small (e.g.  $0.100 \text{ m}^2$ )  $\eta_{\text{fp}}^{\text{tot}}$  is significantly lower compared to the other cases, even for  $p^{\text{REF}} = 50.0 \text{ bar}$ .

### 5.2. Reforming Temperature Analysis

The temperature of the membrane reforming reactor strongly affects the membrane stability [37] and the plant performance [24, 72]. For stability purposes it should be relatively low, while higher  $T^{\text{REF}}$  might improve the reformer performance. For this reason,  $\eta_{\text{fp}}$  is estimated varying  $T^{\text{REF}}$  in the range [590° C, 850° C]. The results reported in Figure 21 are retrieved for  $\dot{m}_{\text{NG}}^{\text{REF}} = 6.90 \text{ kg/h}$ .

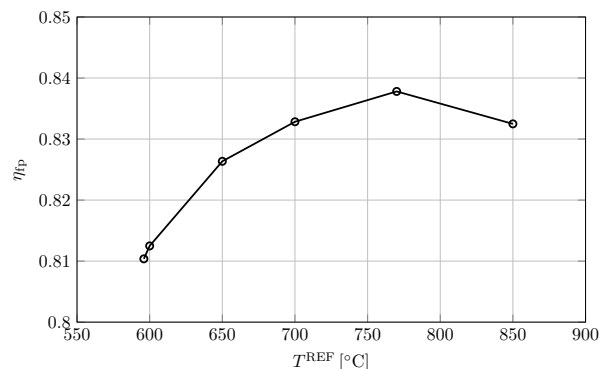


Figure 21: Fuel processor efficiency as a function of the reformer temperature ( $T^{\text{REF}}$ ).

We comment that, for a reforming temperature  $T^{\text{REF}} = 600 \text{ °C}$ , the chemical energy present in the retentate (in the form of un-reacted natural gas and non separated hydrogen) is enough to provide the thermal power necessary for the reforming, without providing additional NG to the burner. As a consequence the system in study cannot be operated at  $T^{\text{REF}} < 600 \text{ °C}$ , otherwise some chemical energy in the retentate should be wasted, leading to a dramatical decrease in the efficiency of the fuel processor.

For  $\dot{m}_{\text{NG}}^{\text{REF}} = 6.90 \text{ kg/h}$ , the pure hydrogen mass flow rate produced varies between  $\dot{m}_{\text{H}_2} = 3.09 \text{ kg/h}$  for a reformer temperature of 770° C, and  $\dot{m}_{\text{H}_2} = 2.22 \text{ kg/h}$  for

a reformer temperature of 600 °C. Thereafter, lowering the temperature reduces the system power density. Moreover,  $\eta_{fp}$  decreases from 83.8 % to 81.2 % by reducing  $T^{REF}$  from 770 °C to 600 °C. Such a performance derating might be acceptable if necessary to use selective membranes integrated in the steam reforming reactor.

A drop in the fuel processor efficiency is observed, from Figure 21, for  $T^{REF} = 850$  °C. In fact, while the yield of reaction (10) is almost constant for temperatures higher than 770 °C, the thermal power necessary to sustain the process increases. As a consequence the natural gas sent to the burner increases, while the pure hydrogen produced remains almost constant.

### 5.3. Pinch Point Analysis

The thermal integration in an endothermic process, such as the production of hydrogen via natural gas steam reforming, is a key aspect to obtain a good efficiency of the fuel conversion. For this reason, the heat exchangers for thermal energy recovery in the fuel processor are crucial elements. In fact, decreasing the pinch point temperature difference would result in a better exploitation of the thermal power available in the hot fluxes. However, such a process entails increasing the cost of the heat exchanger. For this reason, it is interesting to assess the impact of the pinch point temperature difference, of all heat exchangers in the plant, on the efficiency of the fuel processor. The results of such analysis are reported in Figure 22.

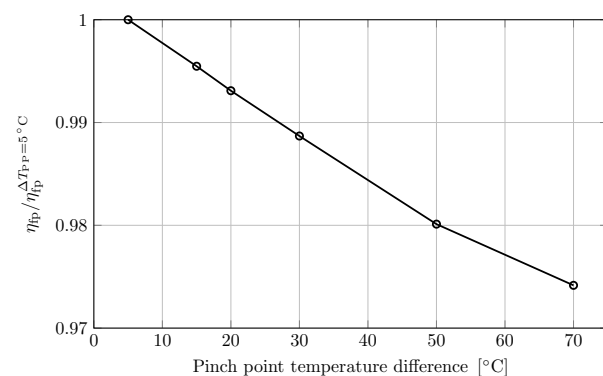


Figure 22: Ratio between the fuel processor efficiency and  $\eta_{fp}$  calculated for a pinch point temperature difference of 5 °C, as a function of the pinch point temperature difference of all heat exchangers in the fuel processor.

Figure 22 shows that a significant correlation between the pinch point temperature difference and the fuel processor efficiency is not present. In fact,  $\eta_{fp}$  decreases only by 3 % by increasing  $\Delta T_{pp}$  from 5 °C to 70 °C.

## 6. Conclusions

In this paper we assess the effects of the integration of Pd-based selective membranes in the fuel processor of a 50 kW<sub>el</sub> PEMFC based CHP system, fed by natural gas. Specifically, we evaluate the following performance indicators: (i) the overall electric efficiency, (ii) the fuel processor efficiency, (iii) and the thermal efficiency. Both design and off-design operating conditions are considered. We use a quasi-lumped parameter approach, integrating Aspen Plus<sup>®</sup> with physical and phenomenological models. We systematically study the integration of selective membranes in the fuel processor, through four case studies. First, we evaluate the performance of a baseline plant, that accounts for steam reforming, water gas shift and syngas purification via pressure swing adsorption unit. Such a system represents the state of the art of PEMFC CHP systems fueled with natural gas. Then, we assess the integration of Pd-based selective membranes as purification unit and integrated both in the water gas shift reactor and in the steam reforming unit. Moreover, detailed analyses are performed on the working parameters, such as the reactors pressure and temperature together with selective membranes surface, of the most innovative fuel processing plant configuration.

The results show that the usage of selective membranes can boost the power plant efficiency. Specifically, the fuel processor nominal efficiency increases from 75.1 %, for the baseline configuration, to 83.8 %, for the fuel processing plant with selective membranes integrated in the steam reformer. As a consequence, the overall electrical efficiency rises from 35.0 % to 38.4 %. This is mainly due the shift of the reforming reaction towards products and to the better thermal integration for heat recovery in reacting fluxes. However, when selective membranes are used as separator or integrated in the water gas shift reactor, the performance boost is minor. In addition, the necessary membrane surface, that largely determine the power plant cost, decreases if the separator is integrated in the reactors. The minimum value of selective membrane area is reached for Plant D configuration, which integrates the membranes into the steam reformer reactor. The real convenience of the improved energy systems studied should be assessed in a real energy management scenario, to thoroughly evaluate the economical and environmental benefits associated to the improved efficiency.

The integration of Pd-based selective membranes leads also to an important fuel processing plant simplification, in particular when the reforming membrane reactor configuration is considered.

At part load, similar conclusions can be made. In fact, the fuel processor efficiency is insensitive to the set-point, while the overall electrical efficiency increases at part load, due to the FC efficiency curve. The thermal efficiency has the opposite behavior. Such trends could be favorable in a real energy management scenario, where the power plant can be often used in off-design conditions (thus at higher electrical efficiency) to meet the user requirements.

In addition, when using Pd-selective membranes integrated in the steam reforming reactor, we found that the optimal working pressure for the system is 35 bar, as a compromise between chemical equilibrium, auxiliary power, and membrane separation efficiency.

The membrane surface is also recognized as a limiting factor to performance, if not properly sized. However, an overestimation could lead to unnecessary additional costs. For these reasons an accurate 2-D or 3-D modeling of the Pd-based selective membranes, also when integrated in reactors could be useful. In fact, phenomena such as the boundary layer formation (i.e. concentration polarisation), or the spatial distribution of the selective membranes in a specific geometry should be investigated. Moreover, several effects such as the how the hydrogen permeance of the membrane varies with temperature could be studied.

To facilitate the integration of selective membranes, the steam reforming reactor can be operated at 600 °C instead of 770 °C, with a fuel processor efficiency decrease of 3.20%. We also comment that for Plant D at 650 – 700 °C, which is well in the range proposed in [60],  $\eta_{fp}$  is still higher compared to the baseline plant. Thus, significant enhancement of fuel processor performance can be obtained also with the current membrane technology through Plant D. We cannot reduce the reformer temperature below 600 °C, as the chemical energy present in the retentate would be enough to sustain the thermal requirements from the endothermic reactions.

It is also important to note that, according to the state of the art technology, selective membranes made by Pd-Ag alloys can operate in a temperature range of (300°C-700°C) [60]. For this reason the technological implementation of Plant D configuration is still questionable. However, from a performance point of view the just cited case is the most relevant, accounting for highest electrical efficiency values. As a consequence, this work focuses on showing the possible advantages related to the selective membranes usage in a CHP energy system, just from the energy performance point of view. Relying on our results we can conclude that the technological development of selective membranes should be

directed towards the extension of the range of possible operating temperatures.

Finally, we underline that the absolute value of the hydrogen permeance of the membrane does not influence the efficiency. On the other hand, the permeance value obviously affects the required membrane area for a certain separation, and thus the economics of the concept, which is not investigated in this paper.

## Acknowledgment

This project has received funding from the Fuel Cells and Hydrogen Joint Undertaking under grant agreement N°671396. This Joint Undertaking receives support from the European Unions Horizon 2020 research and innovation program and United Kingdom, Germany, Greece, Croatia, Italy, Switzerland, Norway. Swiss partners are funded by the State Secretariat for Education, Research and Innovation of the Swiss Confederation.

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